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16-745 Optimal Control and Reinforcement Learning

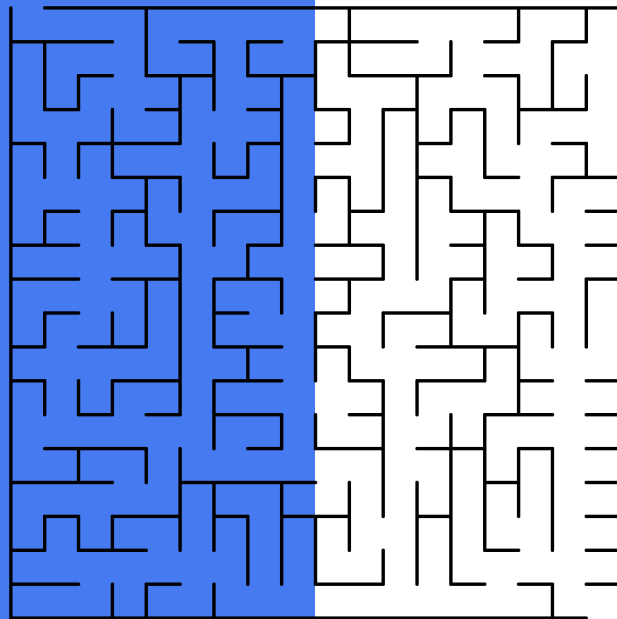
## Trajectory Planning with obstacle avoidance

Team: Into the Unknown

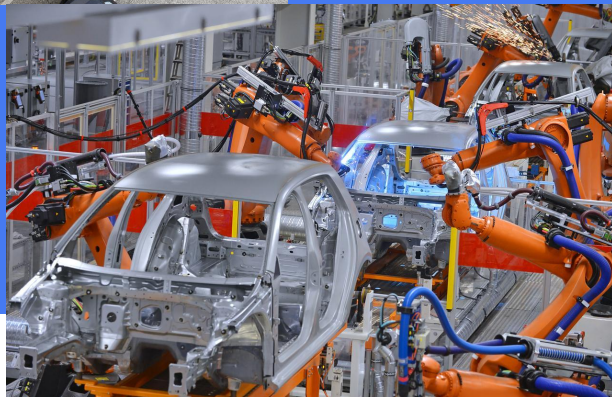
John Zucca (jzucca)

Parv Parkhiya (pparkhiy)

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## Motivation

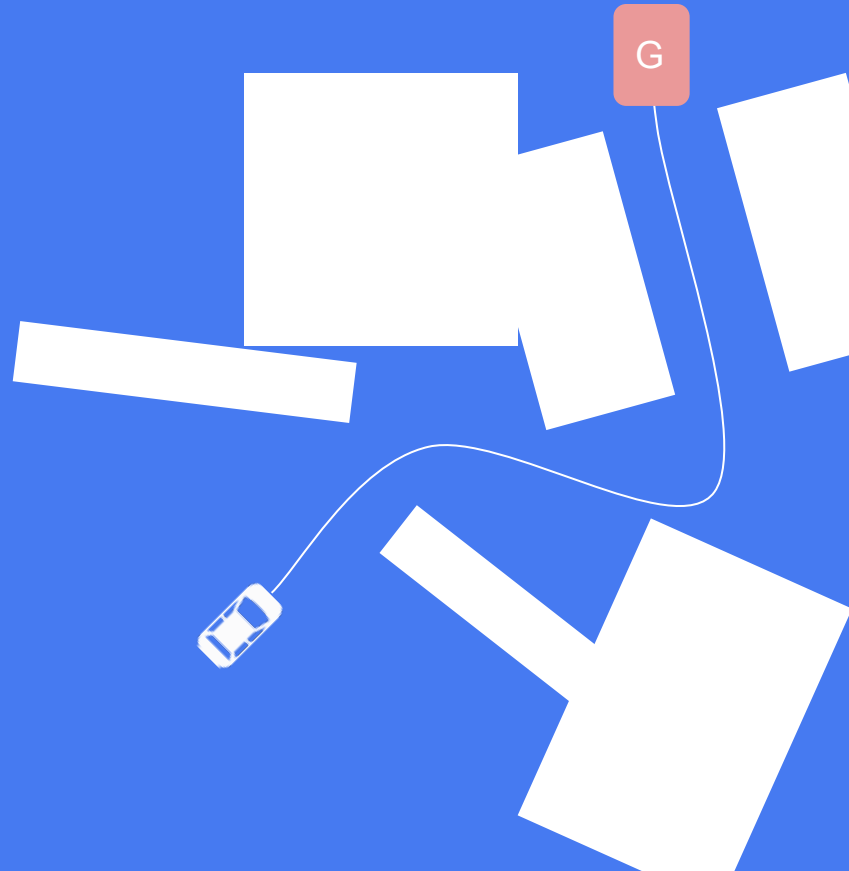
Robots operating in real world will always have plan and replan around the obstacles.

- Parking a Car
  - Manufacturing using manipulator arm
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# Problem Statement

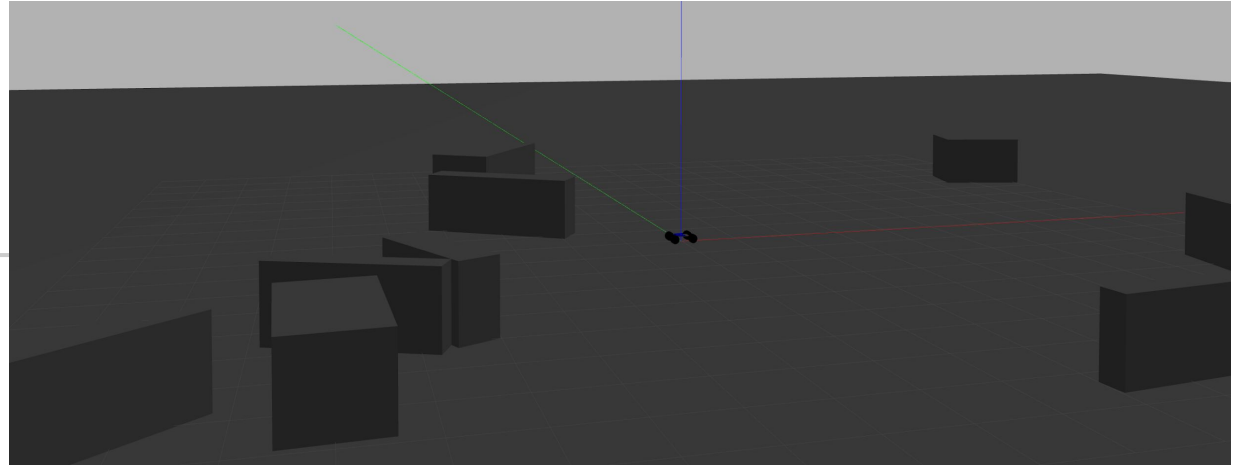
Traverse an Ackermann Vehicle  
from starting position to goal  
position in presence of obstacles

**Goal:**  
Implement and compare classic  
approaches and propose an  
extension



# Overview of the project

Gazebo-ROS  
Environment



*Script to generate a gazebo world with random obstacles*

Approaches

RRT

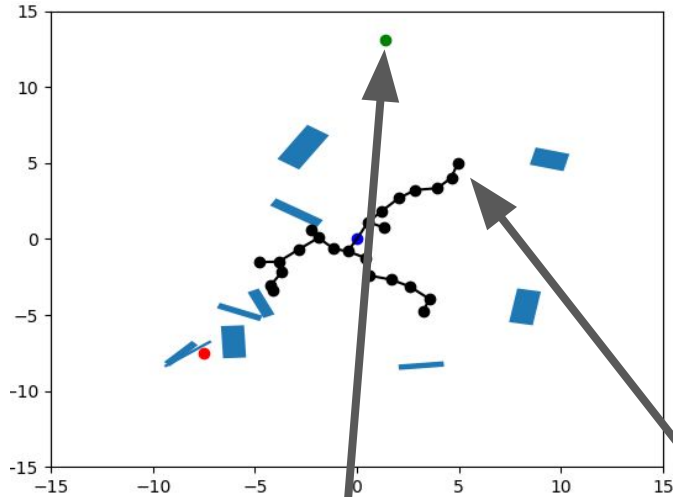
A\*

R\*

Proposed Extension

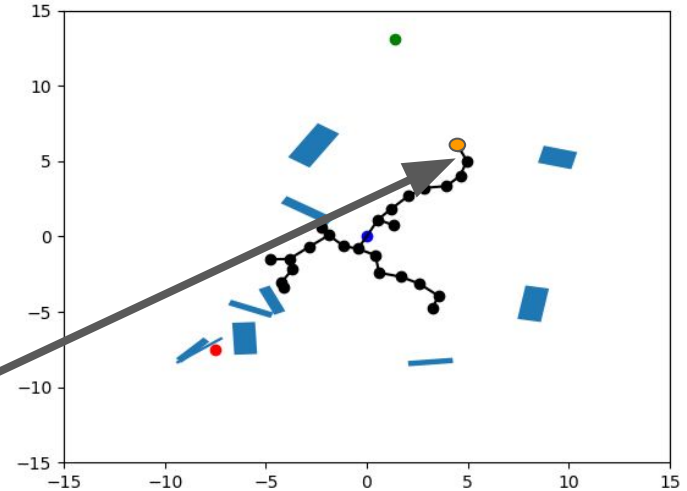
# RRT

## Rapidly Exploring Random Tree

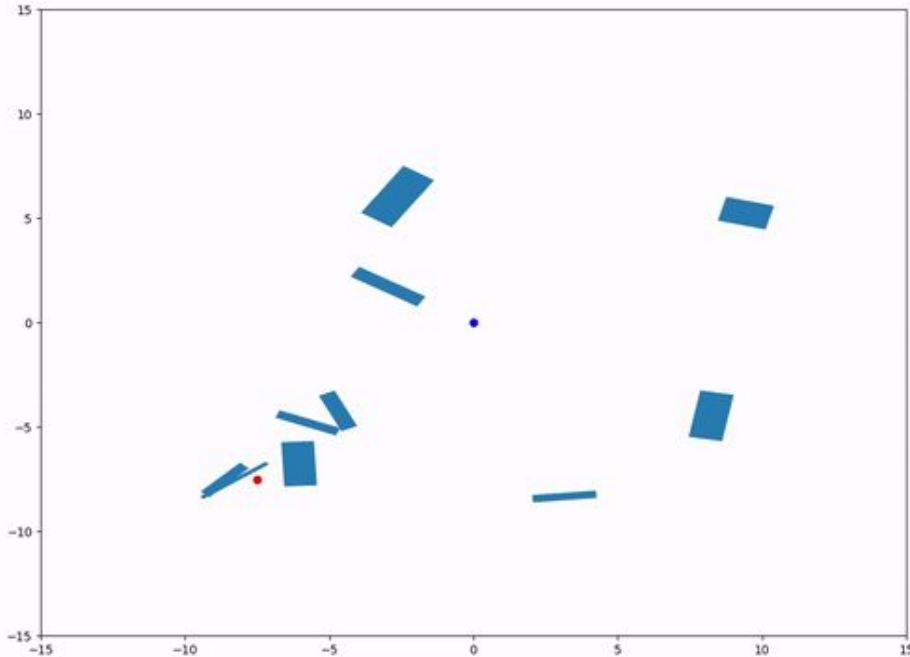


### Growing a tree:

- Sample a random point in the space
- From the existing tree structure find the closest point
- Consider the new edge from closest point in the direction of the sampld point
- If edge's intersection with obstacle is null, add the edge and corresponding node in the tree



# RRT (Implementation)

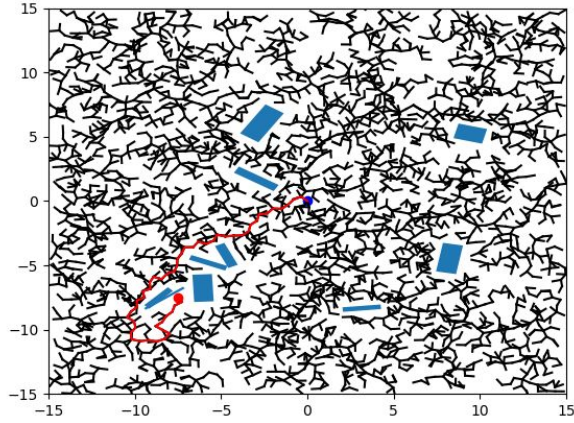


*RRT in action*

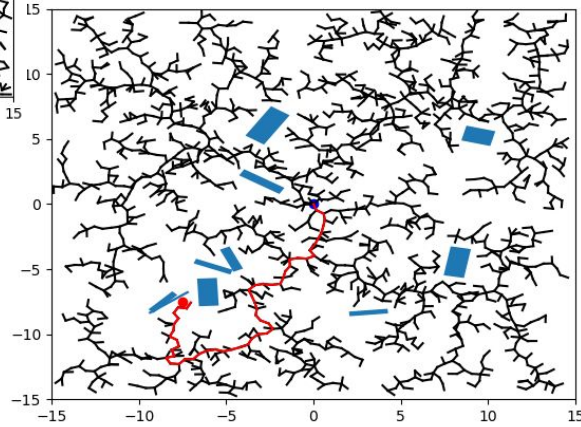
## Key Details:

- Implemented from scratch
- A sampled node is sampled near goal region with some probability (Let's call it goal bias)
- Step length is also randomly sampled each time
- Kd-Tree for efficiently finding the closest node to sampled node
- Occupancy grid for validating new nodes and edge

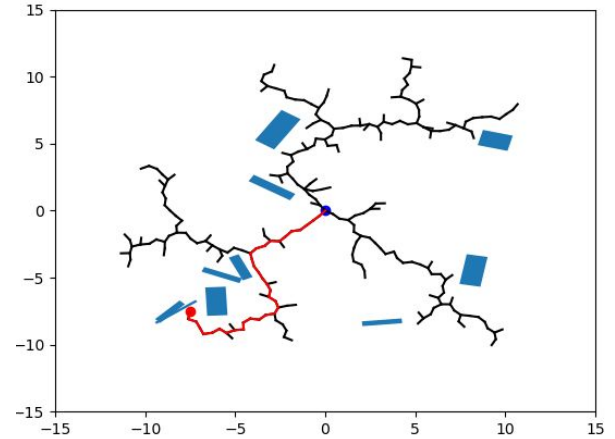
# RRT (Results)



*Without Goal Bias*



*Goal Bias 10%*



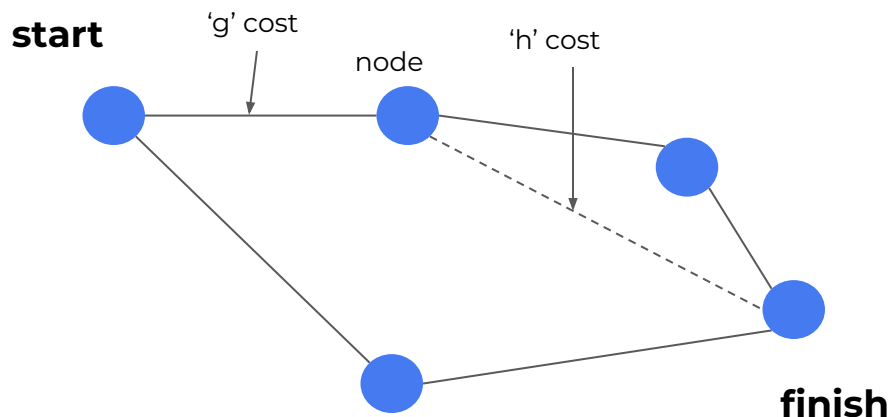
*Goal Bias 25%*



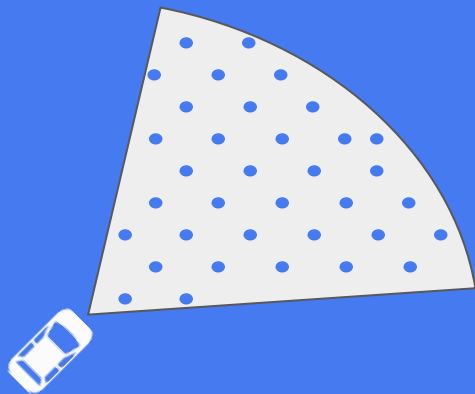
## Creating a trajectory with A\*:

- Maintain two lists of nodes
  - Nodes that have not been explored (open list)
  - Nodes that have been explored (closed list)
- Each node consists of its (x,y) coordinate values and direction theta.
- Each node has two associated costs:
  - From the start node to the current node ('g' cost)
  - Estimated cost (heuristic) to the goal ('h' cost)
- Chose the node from the open list with lowest total cost (g+h) to explore
- Generate a list of successors to this node based on system constraints (e.g. steering angle and obstacles)
- Evaluate the cost functions for these new nodes and add each node to the open list.
- If one of these nodes already exists in the open list and the stored 'g' cost is greater, update this node in the open list, as a cheaper path to this node has been discovered
- Iterate until the goal has been reached

A\*



A\*

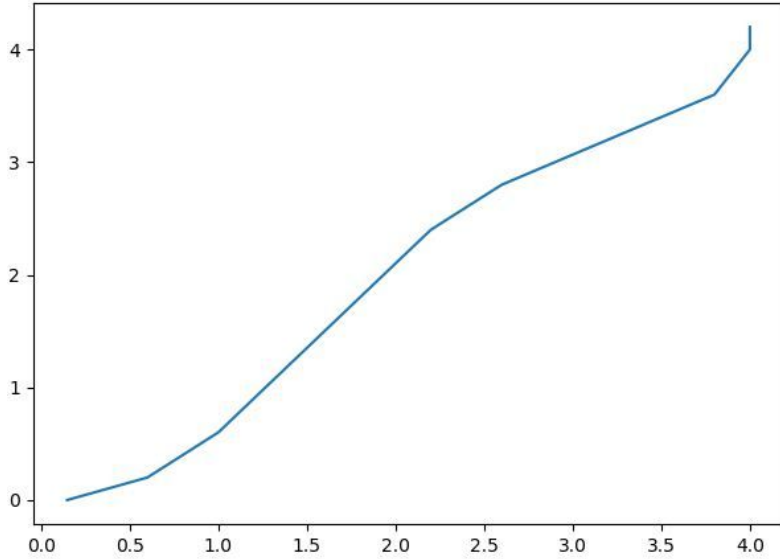


### Key Implementation Details:

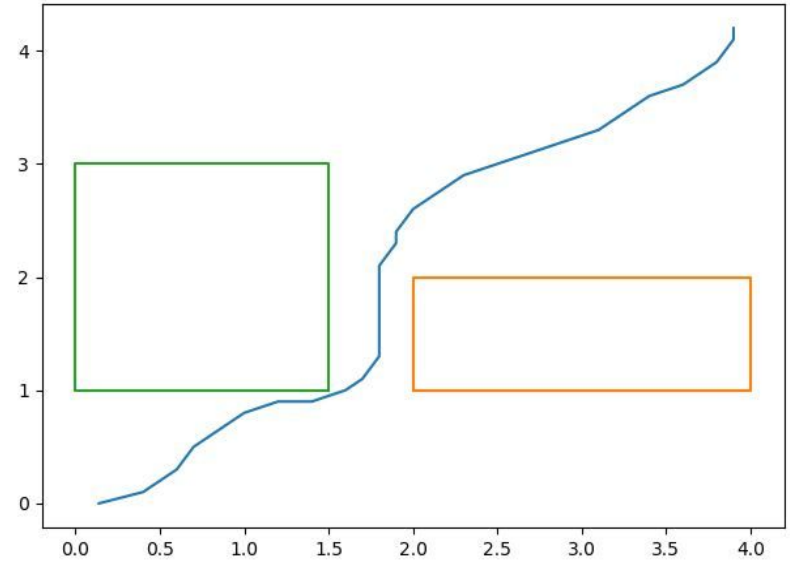
- Implemented from scratch
- (X,Y) grid defined in .1 meter increments
- 'g' cost is defined as euclidean distance
- 'h' cost is defined as  $\sqrt{((\Delta x)^2+(\Delta y)^2+(\Delta \theta)^2)}$
- Allow successor nodes to be up to .5 meters away
- Each node also store its previous node, allowing for simple reconstruction of the trajectory

# A\*

(Results)



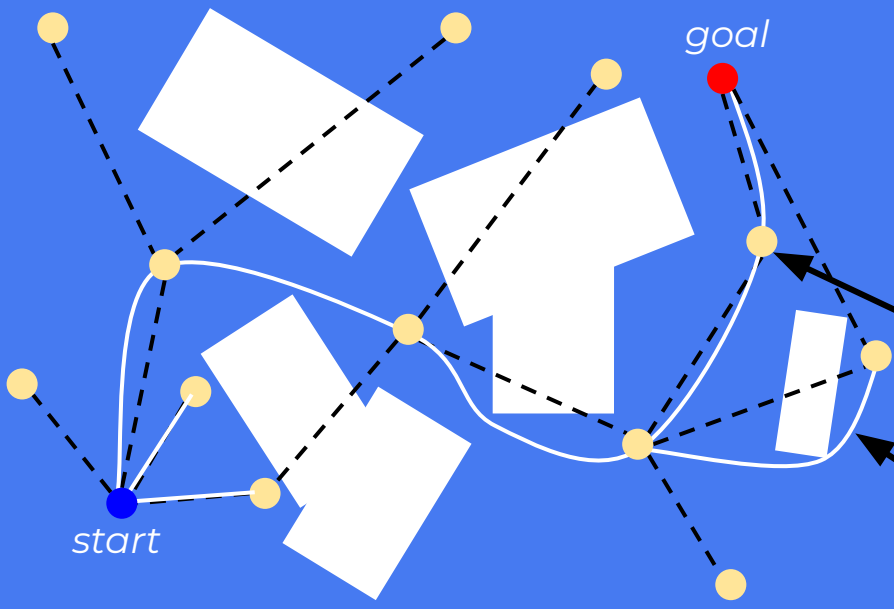
*No Obstacles*



*Multiple Obstacles*

# R\*

(Randomized A\*)



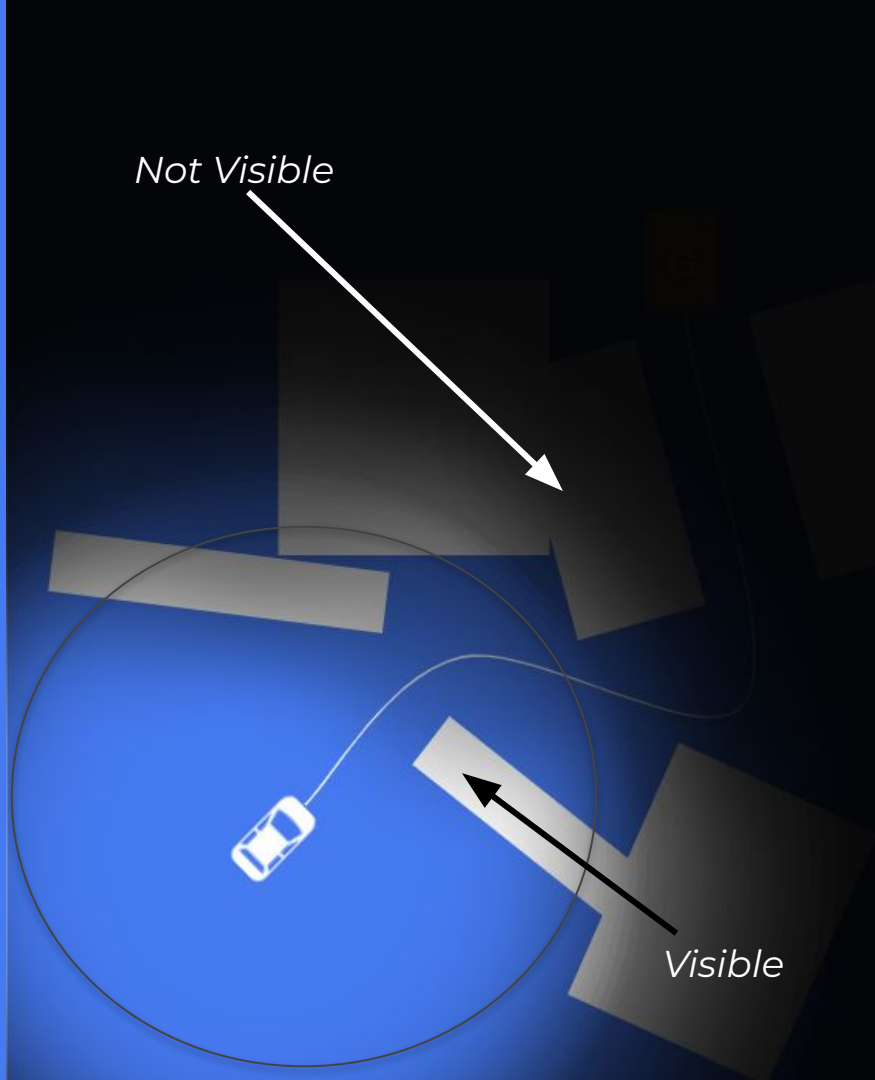
## Key Idea:

- Weighted A\*
  - $f = g + w \cdot h$  (where  $weight(w) > 1.0$ )
- Bounded suboptimal solution ( $w \cdot optimalCost$ ) but can convergence quite early
- Searching at 2 spatial scale level
- High level graph can quickly cover large area but feasible path between them may or may not exist.
- If certain node in the high level graph is found to be promising based on heuristic and cost, then only Low level path is attempted to be calculated using time-bound weighted A\*

# Proposed Extension

## Real Time Trajectory Modification

- In practice, not all obstacles are known prior to driving.
- We must be able to adapt and change our desired trajectories in real time, as new information presents itself
- We aim to limit the obstacles that the vehicle can see during initial trajectory planning, and reveal these obstacles when they are within a defined distance of the vehicle.
- We are likely to use the algorithm that yields the quickest results, as computation time is crucial for this task



RRT:

- Not Optimal At All
- Not Smooth
- Convergence not consistent

A\*:

- Slow(current implementation)
- Smoother than RRT, but still not Smooth
- Consumes A Lot of Memory
- Local Minima takes long
- Lack of precision(fixed grid)

R\*:

- Sub Optimal

Applicable to all:

- Can not react to new obstacles introduced at runtime

## Limitations

## Future Work

A\*:

- Optimization of code for faster runtime
- Further refine cost functions
- Explore utilizing a non-fixed grid

RRT:

- Implementing RRT\* (if time permits)

R\*:

- Full implementation

Proposed Extension:

- Recompute trajectories while vehicle is moving as obstacles are sensed by the vehicle

Applicable to all:

- Integrate with Pure Pursuit controller
- Add width of the vehicle into consideration
- Compare accuracy, trajectory feasibility, and compute time of each implementation

**Questions?**

